

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

	CANDIDATE NAME						
	CENTRE NUMBER		CANDIDATE NUMBER				
* 7 1	MATHEMATICS		0580/41				
5 7	Paper 4 (Extended))	October/November 2010				
°			2 hours 30 minutes				
6	Candidates answer	on the Question Paper.					
0 8 5 *	Additional Materials	s: Electronic calculator Mathematical tables (optional)	Geometrical instruments Tracing paper (optional)				

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.Write in dark blue or black pen.You may use a pencil for any diagrams or graphs.Do not use staples, paper clips, highlighters, glue or correction fluid.DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place. For π use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 130.

This document consists of 16 printed pages.













A farmer makes a rectangular enclosure for his animals. He uses a wall for one side and a total of 72 metres of fencing for the other three sides.

The enclosure has width x metres and area A square metres.

(a) Show that $A = 72x - 2x^2$.

Answer (a)

(b) Factorise completely $72x - 2x^2$.

Answer(b) [2]

(c) Complete the table for $A = 72x - 2x^2$.

x	0	5	10	15	20	25	30	35
A	0	310	520			550	360	

[3]

[2]

(d) Draw the graph of $A = 72x - 2x^2$ for $0 \le x \le 35$ on the grid opposite.





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(a) Calculate the total surface area of the outside of the tank. [The curved surface area, A, of a cone with radius r and slant height l is $A = \pi r l$.]

Answer(a) m^2 [6]

- (b) The tank is completely full of water.
 - (i) Calculate the volume of water in the tank and show that it rounds to 33 m³, correct to the nearest whole number.

[The volume, V, of a cone with radius r and height h is $V = \frac{1}{3}\pi r^2 h$.]

Answer(b)(i)

[4]



- Height (h cm) ≤130 ≤140 ≤150 ≤160 ≤165 ≤170 ≤180 ≤190 Cumulative frequency 0 10 50 95 115 145 180 200 (a) Draw a cumulative frequency diagram to show the information in the table. 200
- 5 The cumulative frequency table shows the distribution of heights, h centimetres, of 200 students.

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(ii) One of the 200 students is chosen at random and then a second student is chosen at random from the remaining students.

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[2]

Calculate the probability that one has a height greater than 170 cm and the other has a height of 140 cm or less. Give your answer as a fraction.

Answer(c)(ii) [3]

(d) (i) Complete this frequency table which shows the distribution of the heights of the 200 students.

Height $(h \text{ cm})$	130< <i>h</i> ≤140	140< <i>h</i> ≤150	150< <i>h</i> ≤160	160< <i>h</i> ≤165	165< <i>h</i> ≤170	170< <i>h</i> ≤180	180< <i>h</i> ≤190
Frequency	10	40	45	20			

(ii) Complete this histogram to show the distribution of the heights of the 200 students.



The diagram shows a toy boat. AC = 16.5 cm, AB = 19.5 cm and PR = 11 cm.Triangles *ABC* and *PQR* are **similar**. (i) Calculate *PQ*.

(ii) Calculate BC.

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(a)

Answer(a)(ii) BC = cm [3]

Answer(a)(i) PQ = cm [2]

(iii) Calculate angle ABC.

Answer(a)(iii) Angle ABC =[2]

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(a)



8	(a)		$\mathbf{f}(x) = 2x - 1$	$g(x) = x^2$			For Examiner's
		Wo	rk out				Use
		(i)	f(2),		Answer(a)(i)	[1]	
		(ii)	g(- 2),		Answer(a)(ii)	[1]	
		(iii)	ff(x) in its simplest for	n,			
		(iv)	$f^{-1}(x)$, the inverse of f(x),	Answer(a)(iii) ff(x) =	[2]	
					Answer(a)(iv) $f^{-1}(x) =$	[2]	
		(v)	x when $gf(x) = 4$.				
	A)		Answ	er(a)(v) x =	or $x =$	[4]	
	(D)	y 15	inversely proportional t	o x and $y = 8$	when $x = 2$.		
		Find (i)	an equation connecting	y and x ,			
		(ii)	y when $x = \frac{1}{2}$.		Answer(b)(i)	[2]	
					Answer(b)(ii) $y =$	[1]	

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(a) The first five terms P_1 , P_2 , P_3 , P_4 and P_5 of a sequence are given below.

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	1	$= 1 = P_1$		Use
	1 + 2	$= 3 = P_2$		
	1 + 2 + 3	$= 6 = P_3$		
	1 + 2 + 3 + 4	$= 10 = P_4$		
	1 + 2 + 3 + 4 + 5	$= 15 = P_5$		
(i)	Write down the next te	erm, P_6 , in the sequence 1, 3, 6, 10, 15		
		Answer(a)(i)	[1]	
(ii)	The formula for the <i>n</i> th	h term of this sequence is		
		$\mathbf{P}_n = \frac{1}{2}n(n+1).$		
	Show this formula is the	rue when $n = 6$.		
	Answer (a)(ii)			
			F13	
(***)	U		[1]	
(111)	Use the formula to find	P_{50} , the 50th term of this sequence.		
		Answer(a)(iii)	[1]	
(iv)	Use your answer to pa	rt (iii) to find 3 + 6 + 9 + 12 + 15 + + 150.		
		Answer(a)(iv)	[1]	
(v)	Find 1 + 2 + 3 + 4 + 5	++ 150.		
		Answer(a)(v)	[1]	
(vi)	Use your answers to p are not multiples of 3.	parts (iv) and (v) to find the sum of the numbers less than 150 w	hich	
		Answer(a)(vi)	[1]	
	Th	nis question continues on the next page.		
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- (b) The first five terms, S_1 , S_2 , S_3 , S_4 and S_5 of a different sequence are given below.
 - $(1 \times 1) = 1 = S_1$ $(1 \times 2) + (2 \times 1) = 4 = S_2$ $(1 \times 3) + (2 \times 2) + (3 \times 1) = 10 = S_3$ $(1 \times 4) + (2 \times 3) + (3 \times 2) + (4 \times 1) = 20 = S_4$ $(1 \times 5) + (2 \times 4) + (3 \times 3) + (4 \times 2) + (5 \times 1) = 35 = S_5$
 - (i) Work out the next term, S_6 , in the sequence 1, 4, 10, 20, 35...

Answer(b)(i) [2]

(ii) The formula for the *n*th term of this sequence is

$$S_n = \frac{1}{6}n(n+1)(n+2).$$

Show this formula is true for n = 6.

Answer(b)(ii)

(iii) Find $(1 \times 20) + (2 \times 19) + (3 \times 18) \dots + (20 \times 1)$.

- Answer(b)(iii) [1]
- (c) Show that $S_6 S_5 = P_6$, where P_6 is your answer to part (a)(i).

Answer(c)

(d) Show by algebra that
$$S_n - S_{n-1} = P_n$$
. $[P_n = \frac{1}{2}n(n+1)]$
Answer(d)

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[1]

[1]

[3]

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